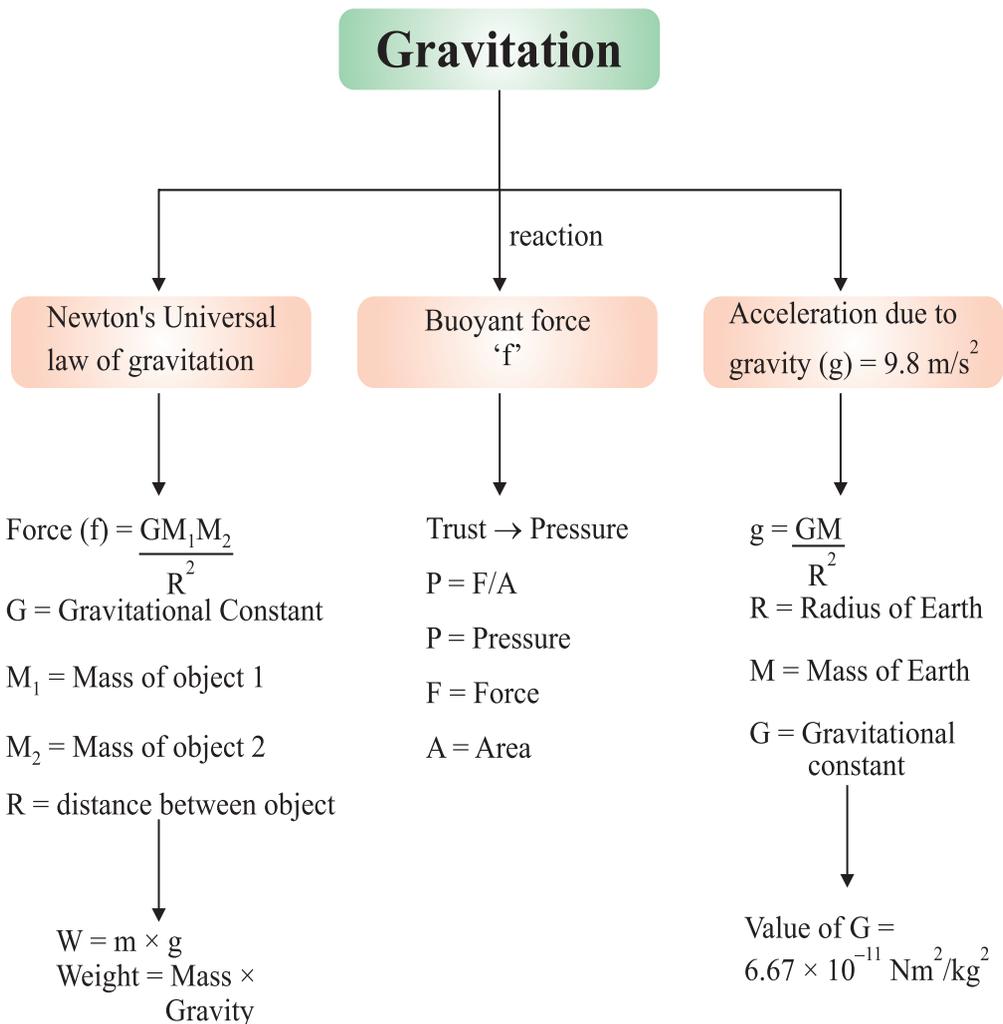


## Chapter - 10

# Gravitation

### CHAPTER AT A GLANCE



## Gravitational Force of Earth

A

If we release a small stone without pushing it from a height, it accelerates towards earth. The stone is when accelerated towards earth, means some force is acting on it.

B

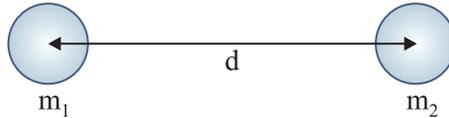
The force which pulls the objects towards the centre of the earth is known as gravitational force of the earth.

Here, stone also attracts earth. It means every object in universe attracts every other object.

↓  
Earth

## Newton's Universal Law of Gravitation

Sir Isaac Newton in 1687 proposed a law about the force of attraction between the two objects in the universe which is known as Newton's law of gravitation.



According to this law :

Every mass in this universe attracts every other mass with a force which is directly proportional to the product of two masses and inversely proportional to the square of the distance between them.

Let masses ( $m_1$ ) and ( $m_2$ ) of two objects are distance ( $d$ ) apart, then force of attraction ( $F$ ) between them

$$F \propto m_1 \times m_2$$

$$F \propto \frac{1}{d^2}$$

$$F \propto \frac{m_1 \times m_2}{d^2}$$

$$F = \frac{Gm_1 \times m_2}{d^2}$$

where  $G$  is a constant and is known as Gravitational constant.

$$\text{Value of } G = 6.67 \times 10^{-11} \text{ Nm}^2/\text{kg}^2$$

$G$  is called universal gravitational constant.

If unit of  $F$  is in Newton,  $m$  is in kg,  $d$  is in metre, then unit of  $G$  can be calculated as :

$$G = \frac{F \times d^2}{m_1 \times m_2} \text{ so unit be } \frac{\text{Nm}^2}{\text{kg}^2} \text{ or } \text{Nm}^2/\text{kg}^2$$

## Relation between Newton's third law of motion and Newton's law of gravitation

According to Newton's third law of motion, "Every object exerts equal and opposite force on other object but in opposite direction."

According to Newton's law of gravitation, "Every mass in the universe attracts the every other mass."

In case of freely falling stone and earth, stone is attracted towards earth means earth attracts the stone but according to Newton's third law of motion, the stone should also attract the earth and really it is true that stone also attracts the earth with the same force  $F = m \times a$  but due to very less mass of the stone, the acceleration ( $a$ ) in its velocity is  $9.8 \text{ m/s}^2$  and acceleration ( $a$ ) of earth towards stone is  $1.65 \times 10^{-24} \text{ m/s}^2$  which is negligible and we cannot feel it.

### **Importance of universal law of gravitation**

- (i) The force that binds us to the earth.
- (ii) The motion of moon around the earth.
- (iii) The motion of earth around the sun.
- (iv) The tides due to moon and the sun.

### **Free fall of an object and acceleration during free fall**

When an object is thrown upward, it reaches certain height, then it starts falling down towards earth. It is because the earth's gravitational force exerts on it.

This fall under the influence of earth is called 'free fall of an object'.

During this free fall direction do not change but velocity continuously changes which is called acceleration due to gravity.

It is denoted by 'g'.

Its unit is same as acceleration  $\text{m/s}^2$ .

### **Gravitational Acceleration and its value at the surface of earth**

The uniform acceleration produced in a freely falling object due to the gravitational force of earth, is called acceleration due to gravity. It is represented by 'g' and it always acts towards the centre of the earth.

#### **Value of 'g' on the surface of earth**

The force acting on an object is

$$F = \frac{GM_e m}{R^2} \quad \dots(i)$$

Where  $M_e$  = Mass of earth

$m$  = Mass of an object

$R$  = Radius of earth

and if acceleration due to gravity is 'g' due to force F then,

$$F = m \times g \quad \dots(\text{ii})$$

Equating (i) and (ii), we get  $m \times g = \frac{GM_e m}{R^2}$

Or  $g = \frac{GM_e}{R^2}$

If  $G = 6.673 \times 10^{-11} \text{ Nm}^2/\text{kg}^2$ ,  $M_e = 6 \times 10^{24} \text{ kg}$ ,  $R^2 = (6.37 \times 10^6)^2$

Then,  $g = \frac{6.6734 \times 10^{-11} \times 6 \times 10^{24}}{(6.37 \times 10^6)^2}$   
 $g = 9.8 \text{ m/s}^2$

### Relationship and difference between 'G' and 'g'

G = Gravitational constant

g = Acceleration due to gravity

$$g = \frac{GM}{R^2}$$

### Difference between G (Gravitational constant) and g (Acceleration due to gravity)

Gravitation Constant (G)	Gravitational acceleration (g)
1. Its value is $6.6734 \times 10^{-11} \text{ Nm}^2/\text{kg}^2$ .	1. Its value is $9.8 \text{ m/s}^2$ .
2. Its value remains constant always and everywhere.	2. Its value varies at various places.
3. Its unit is $\text{Nm}^2/\text{kg}^2$ .	3. Its unit is $\text{m/s}^2$ .
4. It is a scalar quantity.	4. It is a vector quantity.

**Example.** If two stones of 150 gm and 500 gm are dropped from a height, which stone will reach the surface of earth first and why? Explain your answer.

**Ans.** It was Galileo, who first time demonstrated and depicted that the acceleration of an object falling freely towards earth does not depend on the mass of the object.

It can be verified by universal law of gravitation. Let an object of mass  $m$ , is allowed to fall from a distance of  $R$ , from the centre of the earth.

Then, the gravitational force,  $F = \frac{GM_e m}{R^2}$  ( $M_e$  = Mass of the earth)

The force acting on the stone is  $F = m \times a$

So,  $m \times a = \frac{GM_e m}{R^2}$

Or  $a = \frac{GM_e}{R^2}$

So, acceleration in an object falling freely towards earth depends on the mass of earth and height of the object from the centre of the earth. So stones of mass 150 gm and 500 gm will reach the earth surface together.

***Equation of motion when an object is falling freely towards earth or thrown vertically upwards :***

**Case 1.** When an object is falling towards earth with initial velocity ( $u$ ), then

Velocity ( $v$ ) after  $t$  seconds,  $v = u + gt$

Height covered in  $t$  seconds,  $h = ut + \frac{1}{2}gt^2$

Relation between  $v$  and  $u$  when  $t$  is not mentioned :

$$v^2 = u^2 + 2gh$$

**Case 2.** When object is falling from rest position means initial velocity  $u = 0$  (zero), then

Velocity ( $v$ ) after  $t$  seconds,  $v = gt$

Height covered in  $t$  seconds,  $h = \frac{1}{2}gt^2$

Relation between  $v$  and  $u$  when  $t$  is not mentioned :

$$v^2 = 2gh$$

**Case 3.** When an object is thrown vertically upwards with initial velocity  $u$ , the gravitational acceleration will be negative ( $-g$ ), then

Velocity ( $v$ ) after  $t$  seconds,  $v = u - gt$

Height covered in  $t$  seconds,  $h = ut - \frac{1}{2}gt^2$

Relation between  $v$  and  $u$  when  $t$  is not mentioned :

$$v^2 = u^2 - 2gh$$

## Mass

The mass of a body is the quantity of matter contained in it. Mass is a scalar quantity which has only magnitude but no direction.

SI unit of mass is kilogram which is written in short form as kg.

- Mass of a body is constant and does not change from place to place.
- Mass of a body is usually denoted by the small 'm'.
- Mass of a body cannot be zero.

### Weight

The force with which an object is attracted towards the centre of the earth, is called the weight of the object.

$$\text{Force} = m \times a$$

In case of earth,

$$a = g$$

So,

$$F = m \times g$$

But the force of attraction of earth on an object is called its weight (W). So,

$$W = m \times g$$

So, weight is the force and its SI unit is Newton (N). It depends on 'g' and is a vector quantity.

### Relation between 1 kg wt and express it into Newton :

We know that

$$W = m \times g$$

If mass ( $m$ ) = 1 kg,  $g = 9.8 \text{ m/s}^2$ , then

$$W = 1 \text{ kg} \times 9.8 \text{ m/s}^2$$

Or

$$1 \text{ kg wt} = 9.8\text{N}$$

So, the gravitational force of earth that acts on an object of mass 1 kg is called as 1 kg wt.

### Distinguish between Mass and Weight

Mass	Weight
1. We can measure mass of an object by its inertia.	1. Weight = mass $\times$ acceleration or $m \times g$ .
2. The total quantity of matter contained in an object is called mass of an object.	2. The gravitational force by which earth attracts an object is called weight of the object.
3. Mass of the object remains constant at all the places.	3. Weight of the object is different at different places.
4. Measurement of mass is done by using a pan or beam balance.	4. Measurement of weight is done by using a spring balance.

5. Mass does not change even value of  $g$  is zero at any place.      5. Weight of the object becomes zero if  $g$  is zero.

### Factors affecting value of $g$

Earth is not a perfect sphere. The radius of earth increases when we go from pole to equator. Therefore, in most of the calculation, we can take  $g$  as constant at the surface of earth or closer to it. But, as we move away from earth, we can use equation  $g = \frac{GM}{d^2}$  for solving problems.

**Example.** Calculate the value of 'g' at a height of 12800 km from the centre of the earth (radius of earth is 6400 km). Draw its interpretation.

**Solution :** We know that  $g_1 = \frac{GM_e}{(2R_e)^2}$ ,  $R_e = 6400$  km

Weight of the object from the centre of earth = 12800 km =  $2R_e$

$$\therefore g_2 = \frac{GM_e}{(2R_e)^2}$$

Or 
$$\frac{g_1}{g_2} = \frac{G \cdot M_e}{(R_e)^2} \times \frac{(2R_e)^2}{G \cdot M_e}$$

$$\frac{g_1}{g_2} = \frac{4}{1} \quad \text{Or} \quad 4g_2 = g_1$$

So, the value of gravitational acceleration 'g' at a distance of 12800 km from the centre of the earth is  $\frac{1}{4}$ .

The value of gravitational acceleration 'g' decreases with increasing height.

**The weight of an object on moon is one-sixth of the weight on earth.**

Let mass of an object be  $m$ , its weight on earth means the force by which earth attracts it towards the centre.

Now, 
$$F_e = \frac{GM_e m}{R_e^2} \quad \dots(i)$$

where  $G$  = Gravitational constant,  $M_e$  = Mass of the earth,  $m$  = Mass of object,  $R_e$  = Radius of the earth

Weight of an object on moon,

$$F_m = \frac{GM_m m}{R_m^2} \quad \dots(ii)$$

where  $M_m$  = Mass of the moon,  $R_m$  = Radius of the moon

Dividing equation (i) by equation (ii), we get

$$\frac{F_e}{F_m} = \frac{GM_e \cdot m}{R_e^2} \times \frac{R_m^2}{GM_m \cdot m}$$

$$\frac{F_e}{F_m} = \frac{M_e}{M_m} \times \left( \frac{R_m}{R_e} \right)^2$$

We know that mass of earth is 100 times the mass of the moon.

So,  $M_e = 100M_m$

And radius of earth is 4 times the radius of moon.

So,  $R_e = 4R_m$

Then, 
$$\frac{F_e}{F_m} = \frac{100M_m}{M_m} \times \left( \frac{R_m}{4R_m} \right)^2$$

$$\frac{F_e}{F_m} = \frac{100}{1} \times \frac{1}{16}$$

$$\frac{F_e}{F_m} = 6 \text{ times (approx.)}$$

Hence,  $F_e = 6F_m$

### Thrust and Pressure

**Thrust** : The force acting on an object perpendicular to the surface is called thrust.

**Pressure** : The effect of thrust per unit area is called pressure.

$$\text{Pressure (P)} = \frac{\text{Force (F)}}{\text{Area (A)}}$$

SI unit is  $\text{N/m}^2$  or  $\text{Nm}^{-2}$ .

SI unit of pressure is Pascal denoted by 'Pa'.

### Factors on which pressure depends

Pressure depends on two factors :

- (i) Force applied
- (ii) Area of surface over which force acts

*Examples :*

- The base of high buildings is made wider so that weight of walls act over a large surface area and pressure is less.
- School bags are having broad strap so that the weight of school bags fall over a larger area of the shoulder and produce less pressure and becomes less painful.
- The blades of knives are made sharp so very small surface area and on applying force, it produces large pressure and cuts the object easily.
- All liquids and gases are fluids and they exert pressure in all directions.

**Buoyancy**

The upward force experienced by an object when it is immersed into a fluid is called force of buoyancy. It acts in upward direction and it depends on the density of the fluid.

- Force of gravitational attraction of the earth on the surface of the object  $\leq$  buoyant force exerted by fluid on the surface of the object.

**Result :** The object floats.

- Force of gravitational attraction of the earth on the surface of the object  $>$  buoyant force exerted by fluid on the surface of the object.

**Result :** The object sinks.

That is why, all pin sinks and boat/ship floats on the surface of water. (Archimedes' principle)

**Density**

The mass per unit volume is called density of an object. If M is the mass and V is the volume, then density ( $d$ ) is

$$\text{Density } (d) = \frac{\text{Mass } (M)}{\text{Volume } (V)}$$

SI unit =  $\text{kg/m}^3$

**Archimedes' Principle**

It states, when a body is immersed fully or partially in a fluid, it experiences a upward force that is equal to the weight of the fluid displaced by it.

**Applications of Archimedes' Principle :**

- (i) It is used in determining relative density of substances.

(ii) It is used in designing ships and submarines.

(iii) Hydrometers and lactometers are made on this principle.

It is because of this ship made of iron and steel floats in water whereas a small piece of iron sinks in it.

### Relative density

The ratio of the density of a substance to that of the density of water is called relative density.

$$\text{Relative density} = \frac{\text{Density of a substance}}{\text{Density of water}}$$

It has no unit.

### Solved Numericals

**Example 1.** *Relative density of gold is 19.3. The density of water is  $10^3 \text{ kg/m}^3$ . What is the density of gold in  $\text{kg/m}^3$  ?*

**Solution :** Given, Relative density of gold = 19.3

Density of water =  $10^3 \text{ kg/m}^3$

So, Density of gold = Relative density of gold  
 $\times$  Density of water  
 $= 19.3 \times 10^3$

Hence, density of gold  $= 19.3 \times 10^3 \text{ kg/m}^3$ . **Ans.**

**Example 2.** *Mass of  $0.025 \text{ m}^3$  of aluminium is 67 kg. Calculate the density of aluminium.*

**Solution :** Given, Mass of aluminium = 67 kg

Volume of aluminium =  $0.025 \text{ m}^3$

So, Density  $= \frac{M}{V} = \frac{67}{0.025}$

$= 2680 \text{ kg/m}^3$  **Ans.**

**Example 3.** *The mass of brick is 2.5 kg and its dimensions are  $20 \text{ cm} \times 10 \text{ cm} \times 5 \text{ cm}$ . Find the pressure exerted on the ground when it is placed on the ground with different faces.*

**Solution :** Given, Mass of the brick = 2.5 kg

Dimensions of the brick =  $20 \text{ cm} \times 10 \text{ cm} \times 5 \text{ cm}$

So, Weight of the brick (Thrust/Force)

$= F = mg = 2.5 \times 9.8 = 24.5 \text{ N}$

(i) When the surface area  $10 \text{ cm} \times 5 \text{ cm}$  is in contact with the ground, then

$$\begin{aligned}\text{Area} &= 10 \times 5 = 50 \text{ cm}^2 \\ &= \frac{50}{10000} = 0.005 \text{ m}^2\end{aligned}$$

So,

$$\begin{aligned}P &= \frac{F}{A} = \frac{24.5}{0.0050} \\ &= 4900 \text{ N/m}^2\end{aligned}\quad \text{Ans.}$$

(ii) When the surface area  $20 \text{ cm} \times 5 \text{ cm}$  is in contact with the ground, then

$$\begin{aligned}\text{Area} &= 20 \times 5 = 100 \text{ cm}^2 \\ &= \frac{100}{10000} = 0.01 \text{ m}^2\end{aligned}$$

So,

$$\begin{aligned}P &= \frac{F}{A} = \frac{24.5}{0.01} \\ &= 2450 \text{ N/m}^2\end{aligned}\quad \text{Ans.}$$

(iii) When the surface area  $20 \text{ cm} \times 10 \text{ cm}$  is in contact with the ground, then

$$\begin{aligned}\text{Area} &= 20 \times 10 = 200 \text{ cm}^2 \\ &= \frac{200}{10000} = 0.02 \text{ m}^2\end{aligned}$$

So,

$$\begin{aligned}P &= \frac{F}{A} = \frac{24.5}{0.02} \\ &= 1225 \text{ N/m}^2\end{aligned}\quad \text{Ans.}$$

**Example 4.** A force of  $20\text{N}$  acts upon a body whose weight is  $9.8\text{N}$ . What is the mass of the body and how much is its acceleration ?

**Solution :** Given, Force =  $20\text{N}$ , Weight  $W = 9.8\text{N}$

We know,

$$W = mg$$

So,

$$9.8 = m \times 9.8$$

Or

$$m = 1 \text{ kg}\quad \text{Ans.}$$

And,

$$F = ma$$

So,

$$20 = 1 \times a$$

Or

$$a = 20 \text{ m/s}^2\quad \text{Ans.}$$

**Example 5.** A man weighs  $1200\text{N}$  on the earth. What is his mass (take  $g = 10 \text{ m/s}^2$ ) ? If he was taken to the moon, his weight would be  $200\text{N}$ . What is his mass on



# QUESTIONS

## VERY SHORT ANSWER TYPE QUESTIONS (1 Mark)

1. State the universal law of gravitation.
2. Write the formula to find the magnitude of the gravitational force between the earth and an object on the surface of the earth.
3. Is value of  $G$  constant at all the places ?
4. What is the weight of an object of mass 1 kg ? **Ans : 9.8N**
5. A body has weight of 10 kg on the surface of earth. What will be its weight when taken to the centre of the earth ? **Ans : 0**
6. What is the value of gravitational acceleration acting on a free falling object ?
7. What is the value of universal constant  $G$  and its unit ?
8. Why do pin sinks in water ?
9. Name a factor on which  $g$  depends.
10. Name the balance used to measure weight of an object.

## SHORT ANSWER TYPE QUESTIONS (2 Marks)

1. Mass of an object is 1600 gm on the earth. What is its mass on the moon ? Why ? **Ans : 1600 gm**
2. Two objects placed in a room, are not pulling each other. Why ?
3. Name the force responsible for the motion of moon around the earth. How can some objects move around the earth ?
4. State Archimedes' Principle and explain it with example.
5. State two factors on which buoyant force depends.

## LONG ANSWER TYPE QUESTIONS (5 Marks)

1. Density of aluminium is  $2700 \text{ kg m}^{-3}$ . What is its relative density ? Density of water is  $1000 \text{ kg m}^{-3}$ . Define relative density. **Ans : 2.7**
2. A ball is released from a height of 1 metre. What time it will take to reach the surface of the earth ? **Ans : 0.45 s**
3. A ball thrown up, vertically returns to the thrower after 6 s. Find :
  - (a) the velocity with which it was thrown up. **Ans : 29.4 m/s**
  - (b) the maximum height it reaches and **Ans : 4.9 m**
  - (c) its position after 4 s. **Ans : 39.2 m**